

## Two New benchmarks, with Manual Proofs

• (RULES a c -> c, ->= a b, a b ->= ) hand-waving: number of un-matched a is reduced exact: this number is first component of interpretation

 $\begin{array}{lll} a_I(x,y) &=& \text{if } y > 0 \text{ then } (x,y-1) \text{ else } (x+1,0) \\ b_I(x,y) &=& (x,y+1) \\ c_I(x,y) &=& (x,0) \end{array}$ 

is monotone w.r.t. order  $(x_1, y_1) > (x_2, y_2)$  iff  $x_1 > x_2 \land y_1 = y_2$ 

• (RULES a c -> c, ->= a b, b a ->= ) use the very same interpretation as above, but with order:

 $\begin{aligned} & (x_1, y_1) > (x_2, y_2) \quad \text{iff} \quad (x_1 > x_2) \land (y_1 \ge y_2) \land (x_1 - y_1 > x_2 - y_2) \\ & (x_1, y_1) \ge (x_2, y_2) \quad \text{iff} \quad (x_1 \ge x_2) \land (y_1 \ge y_2) \land (x_1 - y_1 \ge x_2 - y_2) \end{aligned}$ 

• is this semantic labeling w.r.t. a (quasi) model over  $\mathbb{N}?$  see also Hofbauer WST'18.

## Questions asked after the talk

- Danger: notation in the paper is misleading: uses ε in two meanings:
  in rule: ε→<sup>=</sup> ab, translated into TRS rule x→<sup>=</sup> a(b(x))
  - ▶ in interpretation: e₁ = (0,0), epsilon denotes the nullary symbol in the leaf of a term (tree) that encodes a string (abc encoded as a(b(c(c))))
- Q: Do you have a theorem about "R/S is looping  $\iff R/S$  has a looping overlap closure"?

A: No. — We have (FSCD19) "SN(R/S)  $\iff$  SN(R/S, ROC( $R \cup S$ ))" (for relative termination, it is enough to consider mixed derivations strarting from right-hand sides of overlap closures)

- Q: Kissat over Minisat—did you measure? A: I guess I did but I did not take detailed notes.
- Q: Why the new solutions (rel11, rel12)?
  A: change in proof search strategy. Matchbox has too many moving, and moveable parts. Changes in strategy expression may have unforseen consequences.

11/11

9/11

## Conclusion/Discussion



so ... I am starting a project verified SRS termination in Agda

10/11