

# Automation for Exercises in Computer Science and Mathematics

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## Example: problem instance

- ▶ topic: terms over a given many-sorted signature,
- ▶ equivalently, type-correct use of an API

write an expression of type `Cherry` , given

```
Pear c;
static Tomato a ( Pear x , Pear y );
static Tomato b
    ( Cherry x , Cherry y , Tomato z );
static Pear d ( Cherry x );
static Cherry e
    ( Tomato x , Tomato y , Pear z );
```

## Example: submission and evaluation

```
infer type for expression: a ( c , d ( c ) )
function declaration is
  static Tomato a ( Pear x , Pear y )
number of arguments matches declaration? Yes.
check argument number 1 [ ... ]
check argument number 2
  infer type for expression: d ( c )
  function declaration is
    static Pear d ( Cherry x )
  number of arguments matches declaration? Yes
  check argument number 1
    infer type for expression: c
    is variable with declaration: Pear c
    has type: Pear
  type of argument matches declaration? No.
```

## Example: Conf. of Instance Generator

- ▶ teacher sets these parameters

```
Conf { max_arity = 3
      , types = [ Apple, Pear
                , Orange, Cherry, Tomato ]
      , min_symbols = 5 , max_symbols = 5
      , min_size = 7 , max_size = 15
      }
```

- ▶ then a generator program will produce problem instances for students

## Example: Polymorphic Typing

```
Give an expression of type
  Fozzie<Kermit, Kermit>
in the signature
  class S {
  static <T2> Piggy<Piggy<Animal>>
    statler ( Piggy<T2> x , Piggy<T2> y );
  static <T2> Kermit waldorf ( Piggy<T2> x );
  static Piggy<Fozzie<Animal, Animal>> bunsen ( );
  static <T2, T1> T1
    chef ( Piggy<Piggy<T2>> x , Piggy<Piggy<T1>> );
  static <T2> Fozzie<Kermit, T2>
    rowlf ( T2 x , Animal y );
  }
S.<Kermit>rowlf
(S.<Fozzie<Animal, Animal>>waldorf
(S.bunsen ( ) ) , ...
```

## More Examples

- ▶ graph “theory”, discrete mathematics:
  - ▶ instance: graph  $G$ ,  
solution: Hamiltonian Circuit in  $G$
  - ▶ instance: graph  $G$ , number  $k$ ,  
solution: conflict-free  $k$ -colouring of  $G$
- ▶ logic:
  - ▶ instance: propositional logic formula in CNF  
solution: a satisfying assignment
  - ▶ instance: formula in 1st order predicate logic  
solution: a model of the formula

## Leipzig autotool — General Design

for each type of exercise:

- ▶ types: Config, Instance, Solution  
(each with pretty-printer, parser, API doc)
- ▶ functions:
  - ▶ grade:  $\text{Instance} \times \text{Solution} \rightarrow \text{Bool}$
  - ▶  $\rightarrow \text{Bool} \times \text{Text}$
  - ▶ describe:  $\text{Instance} \rightarrow \text{Text}$
  - ▶ initial:  $\text{Instance} \rightarrow \text{Solution}$
  - ▶ generate:  $\text{Config} \times \text{Seed} \rightarrow \text{Instance}$

## Leipzig autotool — Components

- ▶ collection of exercise types  
as (stateless) semantics server (XML-RPC)
- ▶ plugin for Olat LMS (learning management system)
- ▶ stand-alone autotool LMS with
  - ▶ data base (problems, students, grades,...)
  - ▶ web front-end (for student, for teacher, ...)
  - ▶ ... display highscores: small/early solutions
- ▶ since  $\approx$  2000, open-source (GPL), Haskell,  
 $\approx$  1500 modules,  $\approx$  15 MB source  
<https://gitlab.imn.htwk-leipzig.de/autotool/all0>

## Leipzig autotool — Applications

at HTWK Leipzig, IMN, since 2003, in lectures on

- ▶ Modellierung (discrete mathematics and logic)
- ▶ Algorithms and Data Structures
- ▶ Automata and Formal Languages
- ▶ Advanced (i.e., Functional) Programming
- ▶ Artificial Intelligence
- ▶ Principles of Programming Languages
- ▶ Theory of Computation
- ▶ Constraint Programming

## Experience - Students, Teachers

- ▶ autotool is: always available, always correct, always patient
- ▶ teaching/grading assistant is: available for few hours a week only (if at all – staff costs money, which we generally don't have)
- ▶ autotool homework exercises prepare students for discussing “real homework” (that is, proofs) in classes

## Experience - Implementation

- ▶ each exercise type is a domain specific language (concrete syntax, abstract syntax, semantics)
- ▶ *implementation* of the grading algorithm (= semantics) is always the easiest part
- ▶ the hard part is the *design*
  - ▶ what type of exercise helps the student to understand a specific concept?
  - ▶ how can we write the instance generator?

## Design Goals for Exercises

- ▶ grading:
  - ▶ should give reasonable explanation for wrong submissions (not just “it's wrong”)
  - ▶ without giving away the correct solution
- ▶ generator:
  - ▶ each instance: non-trivial, but manageable,
  - ▶ set of instances: sufficiently distinct, but of similar difficulty
- ▶ concrete syntax:
  - ▶ Haskell syntax for tuples, lists, records
  - ▶ except: (model) programming languages

## Design Principles for Exercises

- ▶ basic approach: verify property of an object  
example: any NP complete problem, e.g., SAT
- ▶ but this does not check whether the student used a certain algorithm to construct this object
- ▶ several exercise types implement non-deterministic algorithms (= inference systems)  
student has to find an execution path (inference tree, proof), examples:
  - ▶ Resolution (derive empty clause)
  - ▶ Hilbert style deduction (derive formula)
  - ▶ (balanced) search tree operations

## Example: Algorithms on Search Trees

- ▶ instance: AVL trees  $s, t$ , pattern  $p$ , e.g.,  
[Insert 92, \*, \*, \*, \*, Insert 51, \*, Delete 38]  
solution: sequence  $q$  of operations that matches  $p$  and transforms  $s$  to  $t$
- ▶ this exercise is not to implement operations, but to give correct (black-box) implementation so that students can explore their properties
- ▶ underlying design principle: *sudoku*, that is, create “holes” that students have to fill in

## Design Principle: AST Sudoku

- ▶ start from any exercise type with  
*grade*: Instance  $\times$  Solution  $\rightarrow$  Bool
- ▶ build generator that produces correct pairs
- ▶ Instance  $\in$  Term( $\Sigma$ ), Solution  $\in$  Term( $\Gamma$ ), from Term to Pattern: introduce (several)
  - ▶ variables for subtrees
  - ▶ variables for function symbols
- ▶ “sudoku” variant of this exercise:
  - ▶ instance:  $(p_i, p_s) \in$  Pat( $\Sigma$ )  $\times$  Pat( $\Gamma$ )
  - ▶ solution: a correct instance of  $(p_i, p_s)$
- ▶ unlike Sudoku, solution is not necessarily unique

## Sounds Great - I Want This!

- ▶ autotool is free software (GPL):  
you can download, compile, install, use!  
source/instruction: <https://gitlab.imn.htwk-leipzig.de/autotool/all0>
- ▶ TODO (contributions welcome)
  - ▶ translation (most exercises German-only, some English-only, some have both texts)
  - ▶ more exercise types (requires: 1. design skills, 2. Haskell skills)
  - ▶ integration with other LMS (learning management systems)

## Discussion (this slide added after talk)

- ▶ Q: autotool should give feedback based on models of students' learning process (and errors)  
A: Nice to have. Background see <https://www.uu.nl/staff/JTJeuring#tabPublicaties>
- ▶ Q: autotool tutorials for students? A: Concrete syntax is mostly uniform, semantics is discussed in lectures. Students have to adapt to (but that's exactly the point):
  - ▶ use textual input (not graphical)
  - ▶ read and understand error messages
- ▶ Q: tutorials for teachers? A: see <https://gitlab.imn.htwk-leipzig.de/autotool/all0#documentation-papers-talks-theses>

## Discussion: Can this work?

- ▶ some properties are not decidable (equivalence of context free grammars, of programs, ...)
  - ▶ use tests instead (e.g., 1000 shortest strings and 1000 random strings)
  - ▶ do not check the property, but a formal proof of that property (need to define and implement syntax and semantics for proofs)
  - ▶ change the question to use a decidable approximation instead, e.g., program equivalence: forget states, obtain regular trace language